SEMESTER ONE

YEAR 12

MATHEMATICS SPECIALIST
REVISION 1
UNIT 3

2016

Section One
(Calculator–free)

Name: _____

Teacher: _____

TIME ALLOWED FOR THIS SECTION

Reading time before commencing work: 5 minutes
Working time for section: 50 minutes

MATERIAL REQUIRED / RECOMMENDED FOR THIS SECTION

To be provided by the candidate
Standard items*:* pens, pencils, pencil sharpener, highlighter, eraser, ruler.
Special items: nil.

IMPORTANT NOTE TO CANDIDATES
No other items may be taken into the examination room. It is **your** responsibility to ensure that you do not have any unauthorised notes or other items of a non–personal nature in the examination room. If you have any unauthorised material with you, hand it to the supervisor **before** reading any further.

To be provided by the supervisor
Question/answer booklet for Section One.
A formula sheet which may also be used for Section Two.

Structure of this examination

	Number of questions available	Number of questions to be answered	Working time (minutes)	Marks available	Percentage of exam
Section One Calculator—free	**5**	**5**	**50**	**50**	**35**
Section Two Calculator—assumed	11	11	100	100	65
			Total marks	150	100

Instructions to candidates

1.   The rules for the conduct of this examination are detailed in the Information Handbook. Sitting this examination implies that you agree to abide by these rules.

2.   Write your answer in the Question/Answer booklet.

3.   You must be careful to confine your responses to the specific questions asked and to follow any instructions that are specific to a particular question.

4.   Spare pages are provided at the end of this booklet. If you need to use them, indicate in the original answer space where the answer is continued i.e. give the page number.

5.   Show all your working clearly. Your working should be in sufficient detail to allow your answers to be checked readily and for marks to be awarded for reasoning. Incorrect answers given without supporting reasoning cannot be allocated any marks. For any question or part question worth more than two marks, valid working or justification is required to receive full marks. If you repeat an answer to any question, ensure that you cancel the answer you do not wish to have marked.

6.   It is recommended that you **do not use pencil**, except in diagrams.

7.   The Formula Sheet is **not** to be handed in with your Question/Answer booklet.

1.   (10 marks)

(a)   Try to solve the following system of equations using Gaussian elimination and give a geometric interpretation of your result.   (4)
$$x + y + z = 2$$
$$x - y + z = 6$$
$$x + z = 4$$

(b)   Explain why there is no intersection of the planes
$$x + y + z = 2$$
$$x - 2y + 2z = 6$$
$$-x - y - z = 1$$
(2)

(c)   Use Gaussian elimination to solve the system of equations
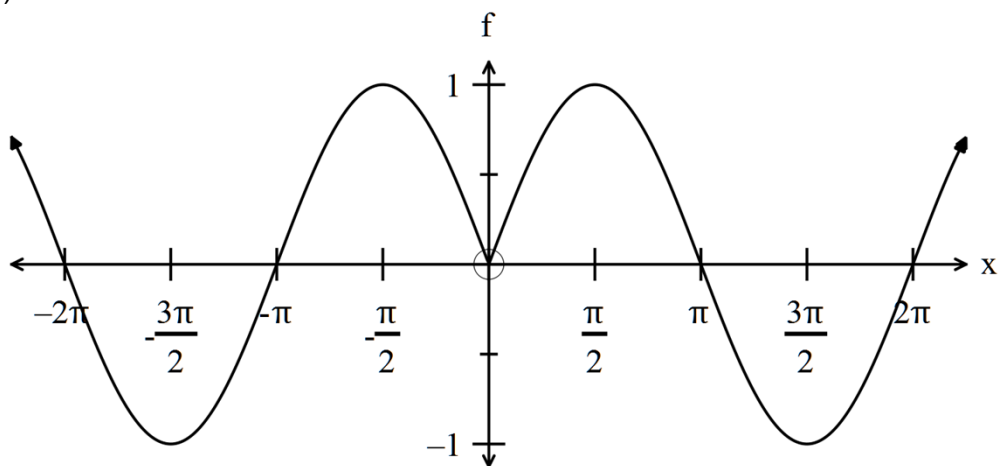$$x + y + z = 6$$
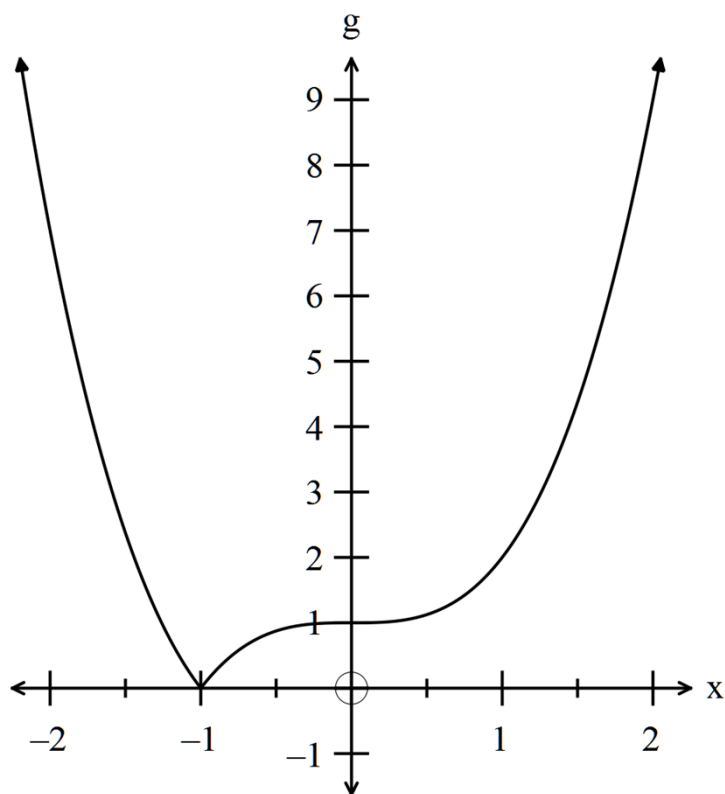$$2x + y - z = 1$$
$$3x - y - z = -2$$
(4)

2.   (6 marks)

Write down the equations of the functions graphed below.

(a)   (2)

$f(x)$ =

(b)   (2)

$g(x)$ =
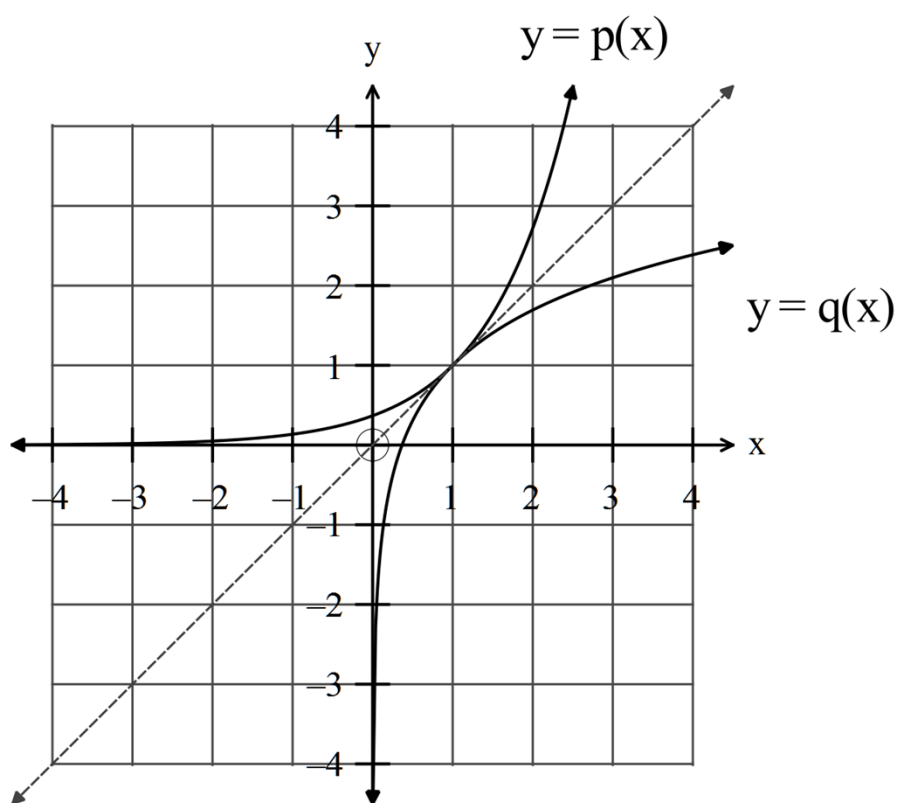
(c)   (2)
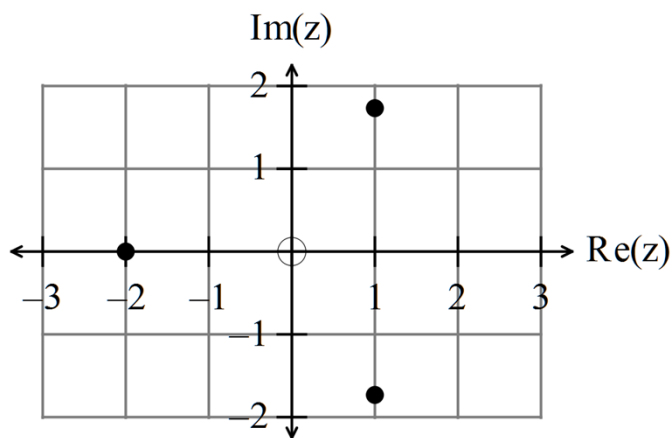

$p(x) =$

$q(x) =$

3.   (13 marks)
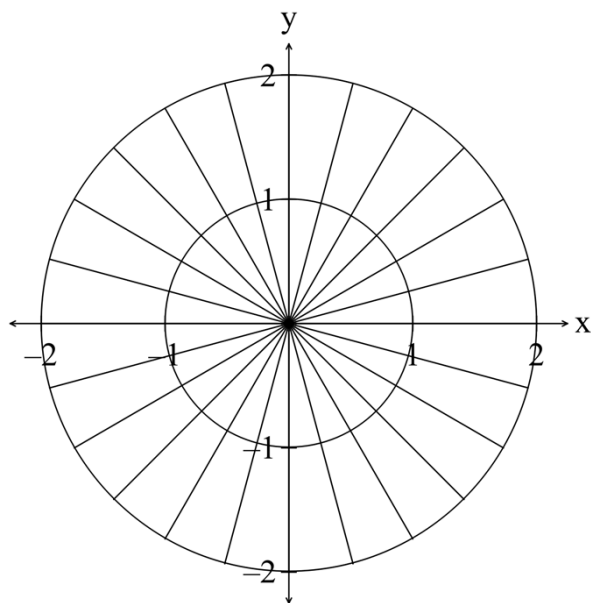
(a)   Solve the equation $z^3 - z^2 - 4 = 0$.   (4)

(b)   Find the complex equation that has roots graphed on the set of axes below.

(3)

(c)   (i)   Sketch the solutions to the equation $z^6 = 1$ on the set of axes below.   (2)
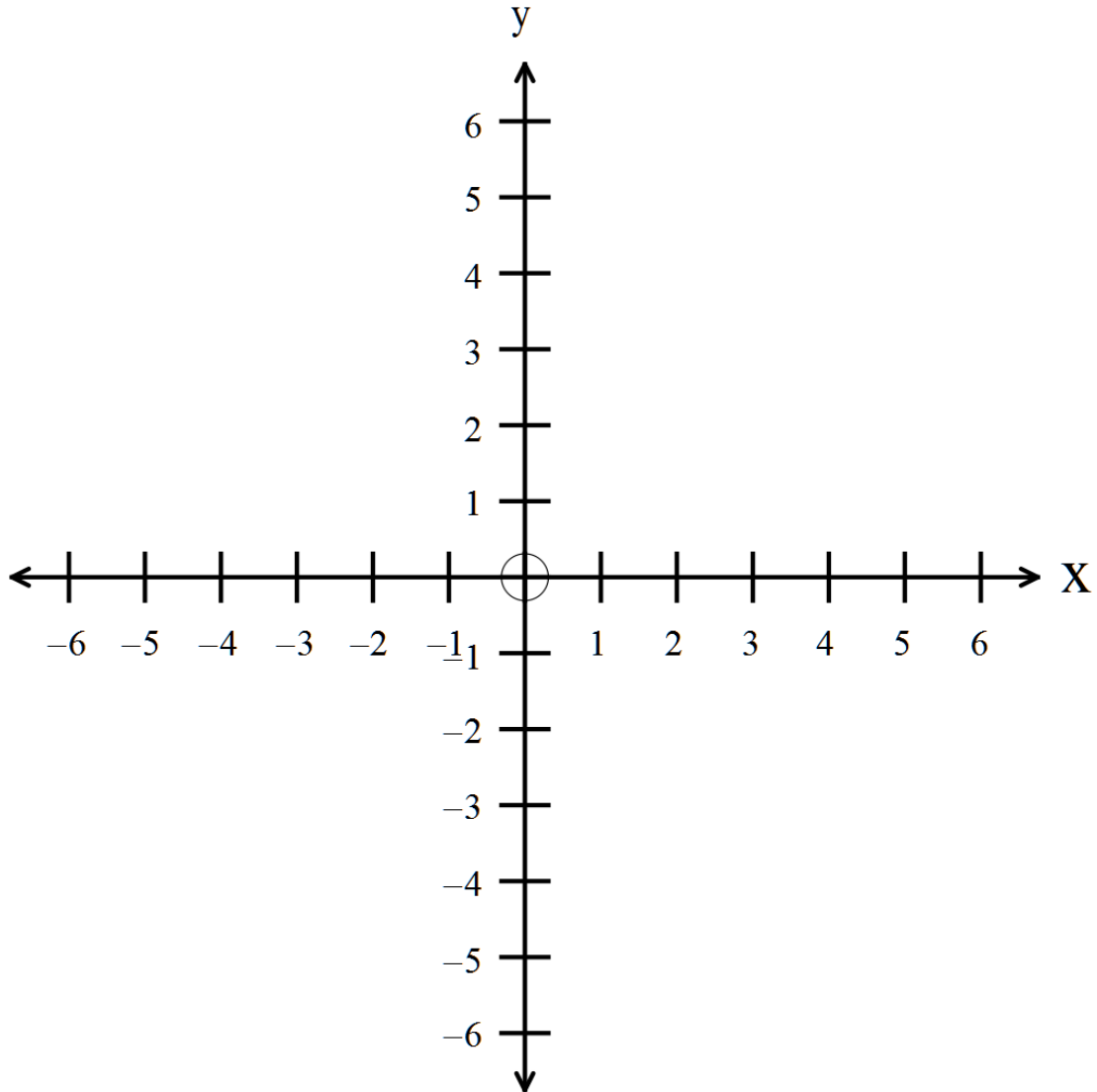

(ii)   Confirm the roots to the equation $z^6 = 1$ algebraically.   (4)

4.   (8 marks)

(a)   Sketch the function $f(x) = \dfrac{(x+3)}{(x+1)(x-3)}$ showing any asymptotes and

intercepts on the set of axes below.   (4)
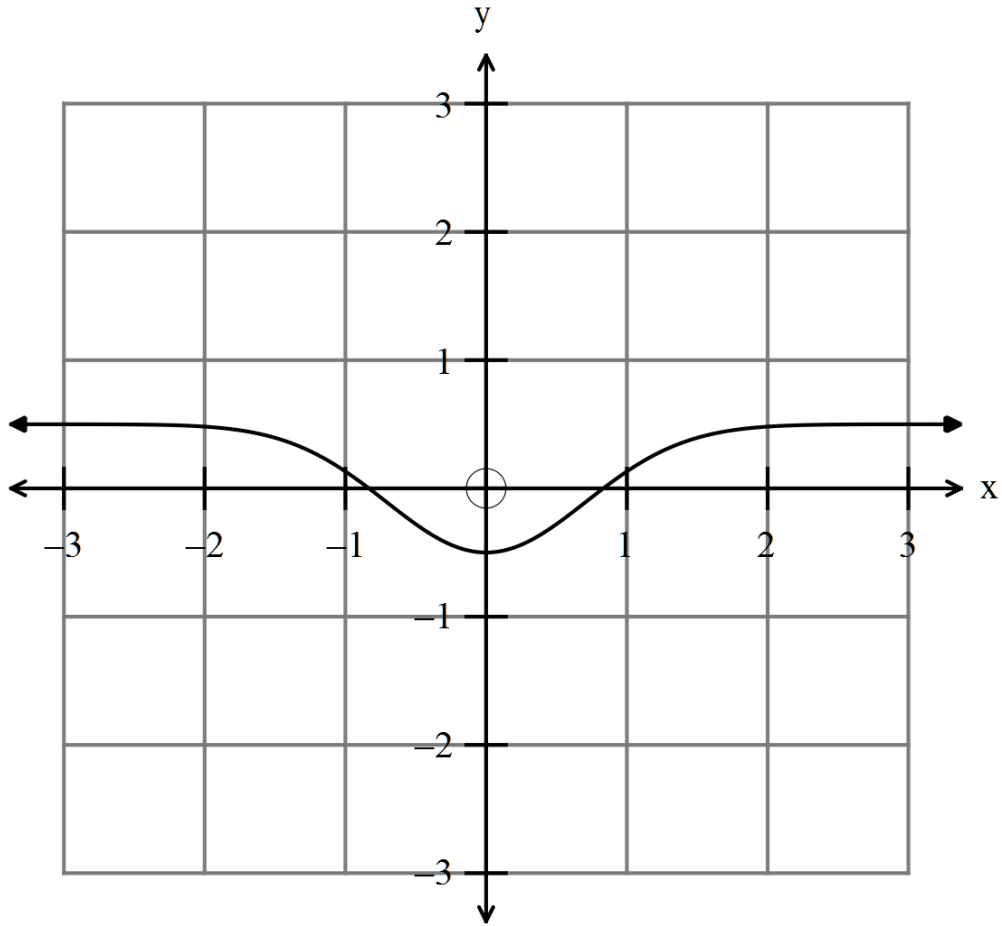
(b)   The function $g(x) = 0.5 - e^{-x^2}$ is sketched on the set of axes below.

Sketch $y = \dfrac{1}{g(x)}$ on the set of axes below.   (4)
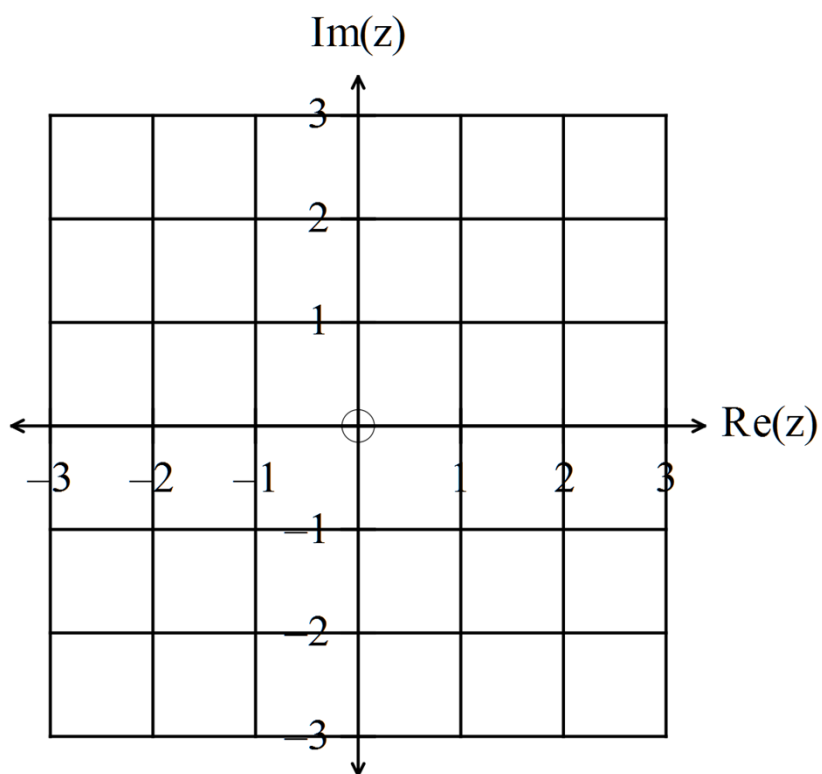
5.   (13 marks)

(a)   Simplify $\left(3\sqrt{3}+\sqrt{2}i\right)\left(2\sqrt{3}-2\sqrt{2}i\right)$.   (3)

(b)   Shade $\left\{z:1<\left|z-i\right|\leq 2\cap \pi \leq arg\left(z\right)\leq 2\pi\right\}$ on the set of axes below.   (3)

(c)   Simplify $(1-i)^{10}$ (2)

(d)   Find $Re\left(\dfrac{3-4i}{1+2i}\right)$ (2)

(e)   If $z = cis\left(\dfrac{2\pi}{3}\right)$

     find

    (i) $\bar{z}$ (1)

    (ii) z^2 (1)

    (iii) $\dfrac{1}{z^2}$ (1)

END OF SECTION ONE